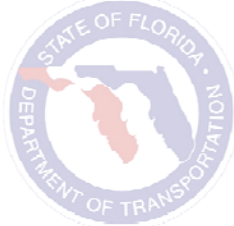



## Modeling Express Lanes Using Dynamic Traffic Assignment Models



Yi-Chang Chiu, PhD

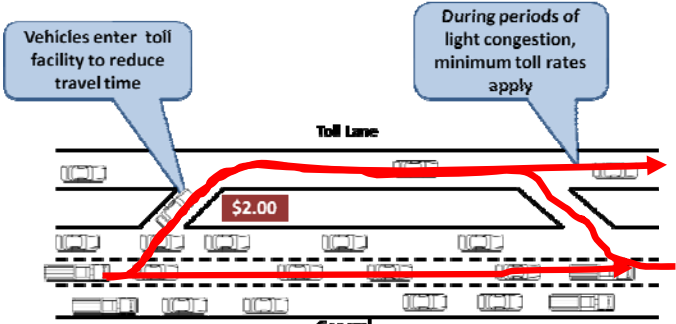
DynusT Laboratory  
University of Arizona

Florida DOT Managed Lane Workshop  
May 22, 2013



## DTA Assumptions

- By using DTA, you accept the following assumptions
  - Estimating lane demand is a **route/departure** choice, not a mode choice problem.



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Credit: Jeff Shelton, TTI

General Purpose

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## DTA Assumptions

- By using DTA, you accept the following assumptions
  - **Learning** and **adaptation** is part of route choice decisions (in lieu of instantaneous or reactive route choice behavior).

```

graph LR
    Day1[Day 1] -- Try --> Day2[Day 2]
    Day2 -- Learn --> Anticipate[Anticipate]
    Anticipate --> DayN[Day n (final)]
  
```


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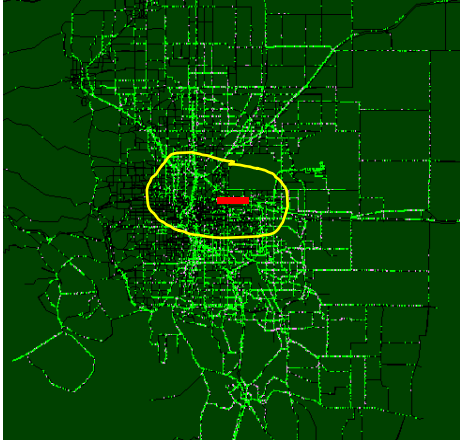
## DTA Components for Pricing Analysis

- **Pricing** model (optional, depending on pricing scheme)
- **Route/lane choice** model
- **Departure time choice** model
  - Developed separately
  - Loop back to demand model
- Network needs to large enough to include most trips through the facility. **A small area over-penalizes tolled facility.**


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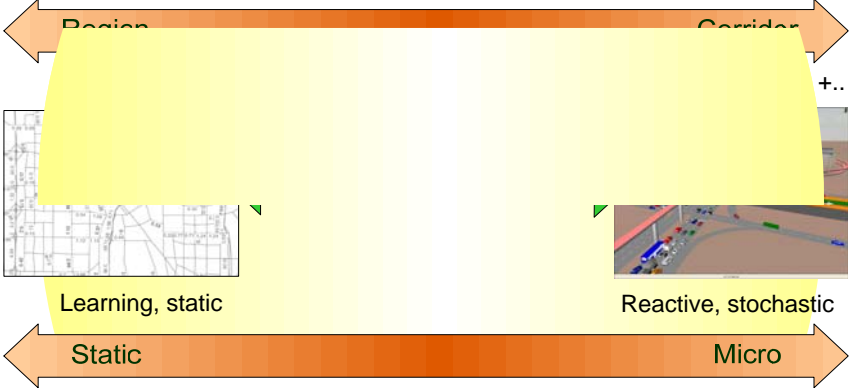
 **Sub-Area Scope Implication**



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 **Why DTA for Express Lane Analysis Given We have had Macro-Micro**

- Macro-Micro inconsistency
  - Traffic dynamic, route choice behavior



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## Why DTA for Express Lane Analysis Given We have had Macro-Micro

- Better consistency with Macro-Meso-Micro integration

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## Why DTA for Express Lane Analysis Given We have had Macro-Micro

- Critical Bridge from Macro to Micro and feedback

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## Pricing Schemes in Real World

- Samples of a wide range of configurations

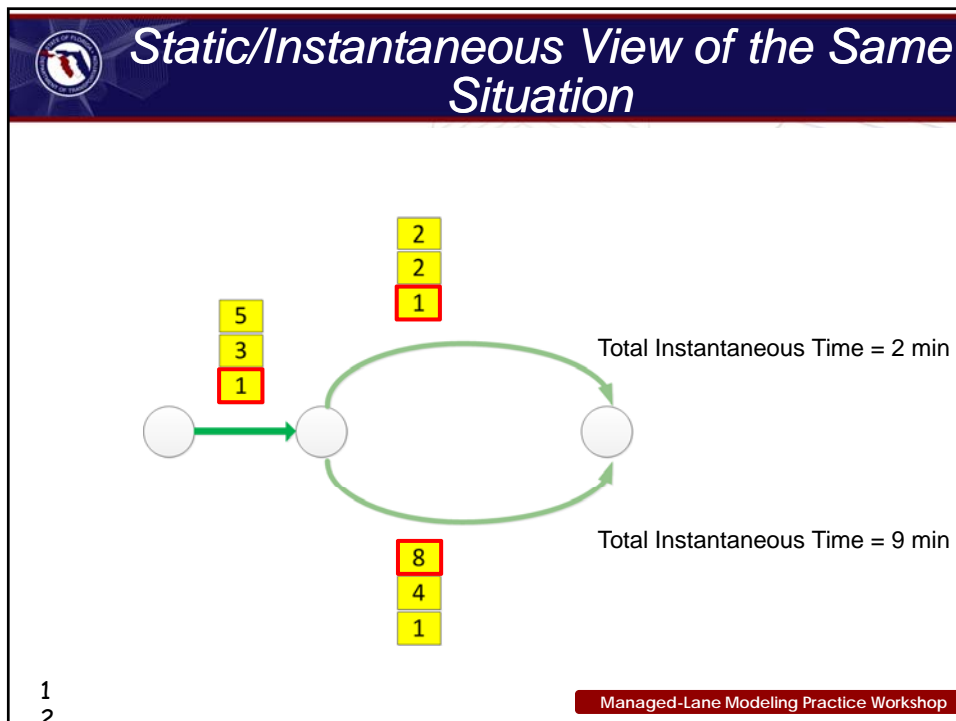
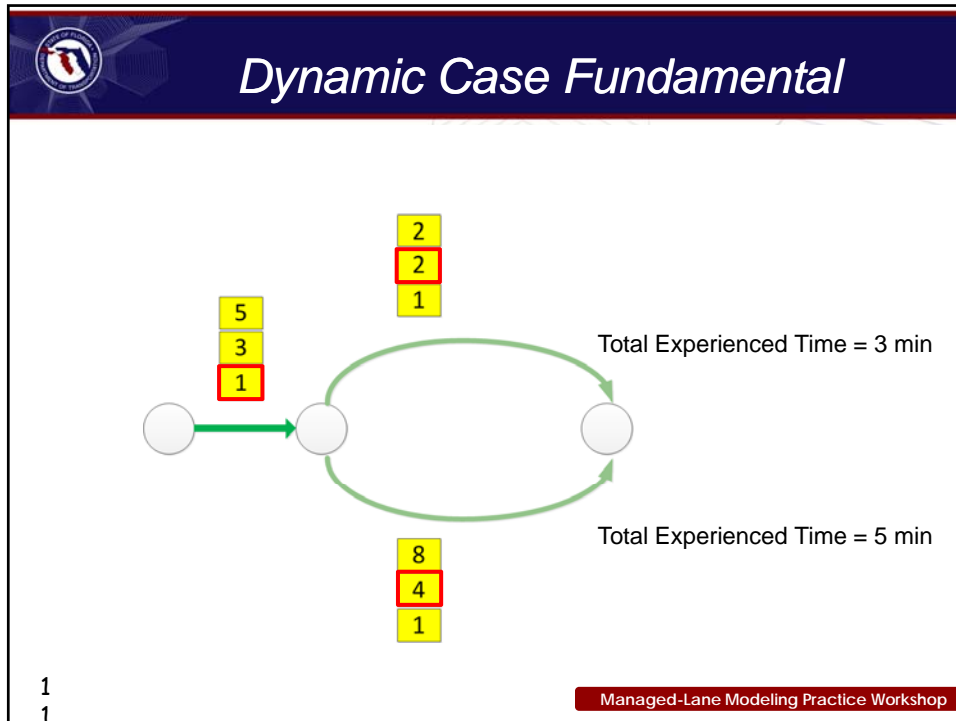
	Facility	HOV	SOV/Two-Axial	Commercial/3 + Axial
DUE	HOV Lanes	✓ (Free)	⊗ (Very High)	⊗ (Very High)
	Toll Roads - Fixed rate - ToD rate	✓ (Free/Normal/ Low)	✓ (Normal)	✓ (High)
DUE/ Non-Eq	Managed Lanes - Fixed rate - ToD rate - Congestion Responsive	✓ (Free)	✓ (Varying)	⊗ (Varying, higher)

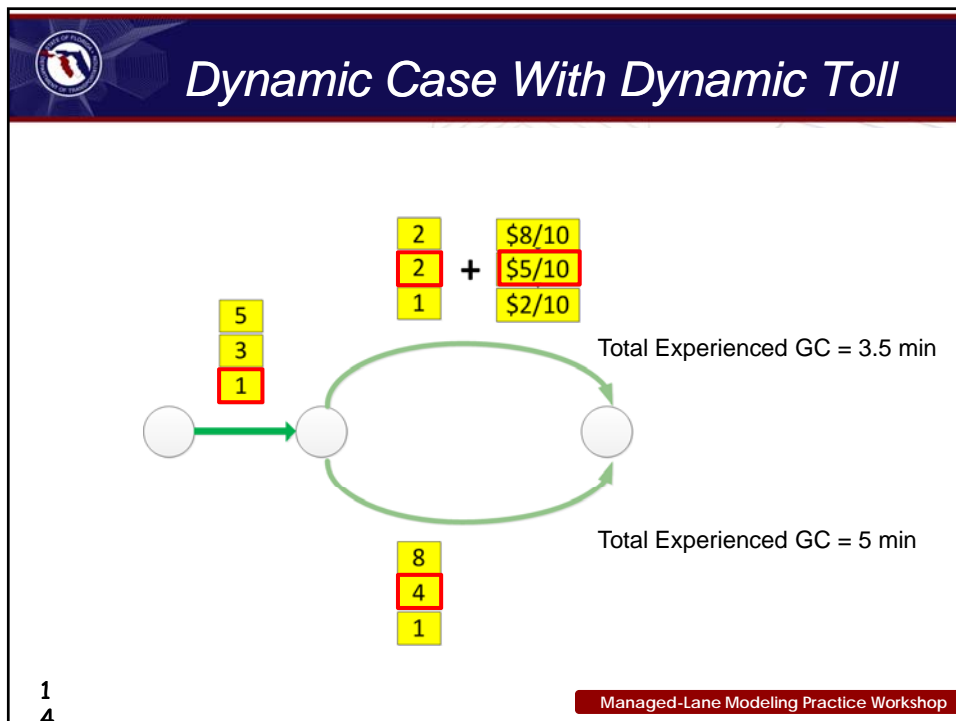
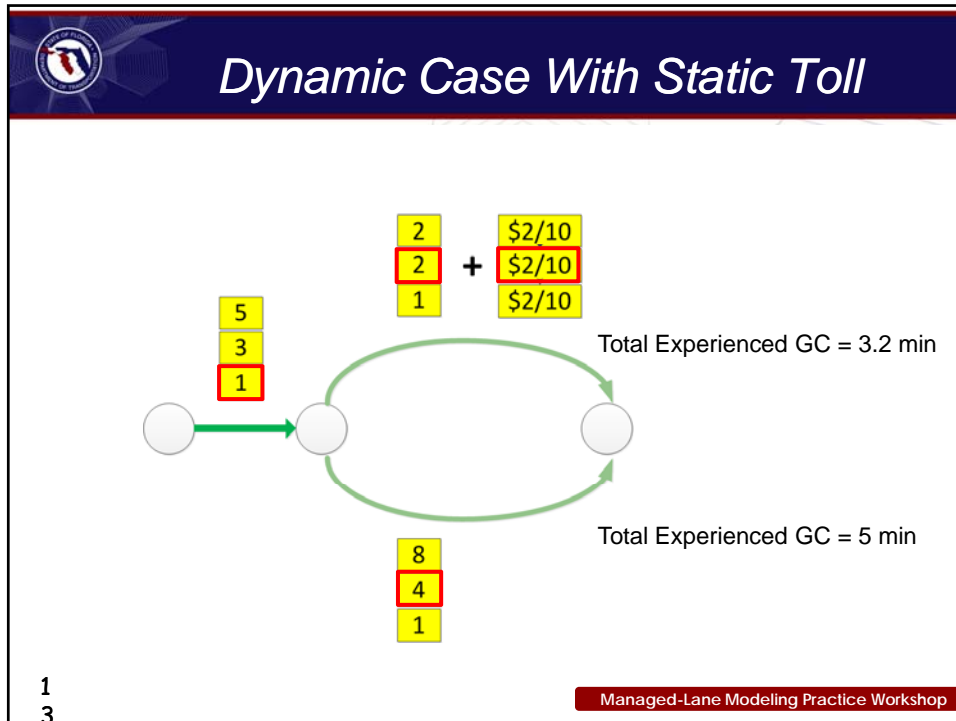
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## Analyzing Tolling in a Simple Static Case

$T1(100) = 20 \text{ min}$        $T1(100||\$1) = 20 \text{ min} + \$1/10 \cdot 60 = 26 \text{ min}$   
 $T2(50) = 20 \text{ min}$        $T2(50) = 20 \text{ min}$   
 $T1(80||\$1) = 17 \text{ min} + \$1/10 \cdot 60 = 23 \text{ min}$   
 $T2(70) = 23 \text{ min}$

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## Revenue/Throughput Maximizing Pricing Model

- Pricing Model (vary by software)**

+

\$8/10
\$5/10
\$2/10

←

$$\max Z = \sum_{l \in L} \sum_{t \in T} k_l^t v(k_l^t)$$

*Subject to,*

$$v(k_l^t) \geq v_l^0, \quad \forall l \in L, t \in T$$

$$\frac{d_l}{\theta_n} \left( \frac{1}{\bar{v}_l^t} - \frac{1}{v(k_l^t)} \right) \leq \pi, \quad \forall l \in L, t \in T$$

$$\frac{d_l}{\theta_n} \left( \frac{1}{\bar{v}_l^t} - \frac{1}{v(k_l^t)} \right) \geq \pi - \varepsilon, \quad \forall l \in L, t \in T$$

*Other DUE Conditions*

*Where,*

- $k_l^t$  : density of CP segment  $l$  at time  $t$
- $v_l^0(k)$  : speed of CP segment  $l$  at time  $t$
- $v_l^0$  : required minimal operating speed inside HOT lane
- $\bar{v}_l^t$  : average speed on the GP lane
- $d_l$  : distance of the CP segment  $l$
- $\pi_l^t$  : toll rate for CP segment  $l$  at time  $t$ ; this is the decision variable.
- $\theta_n$  : value of time for vehicle type  $n$
- $\varepsilon$  : threshold

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## Congestion Responsive Tolling

**Toll Lane**

**General Purpose**

Credit: Jeff Shelton, TTI

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## Congestion Responsive Tolling

As congestion builds, speeds in toll lanes decreases

If speed on toll lanes drops below 45 mph, toll rate increases

Algorithm updates toll rates in 5 minutes intervals

**Toll Lane**

**General Purpose**

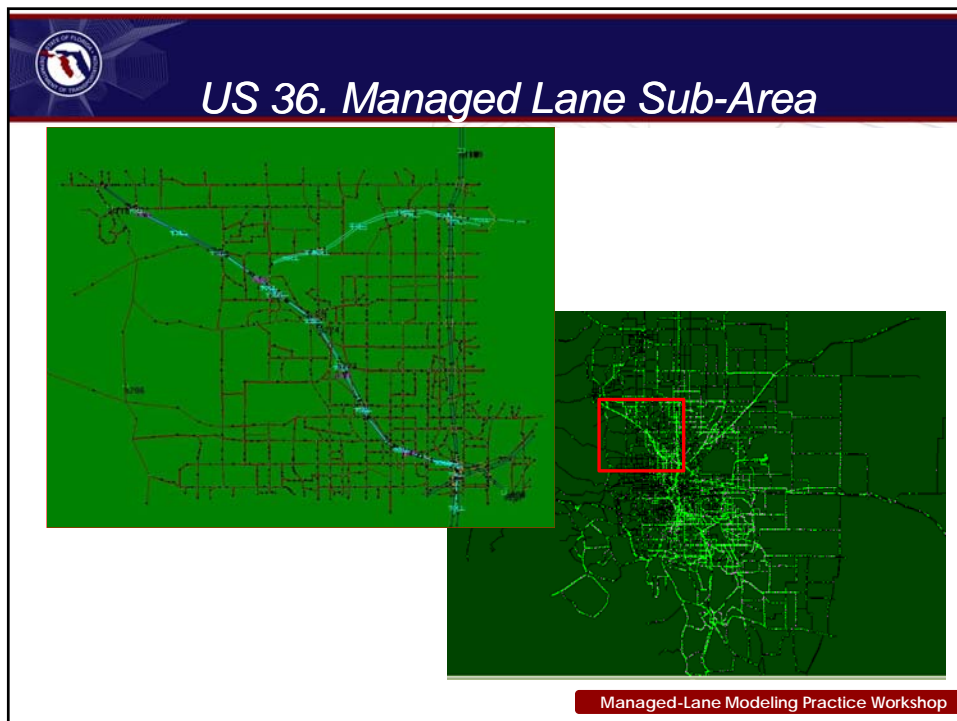
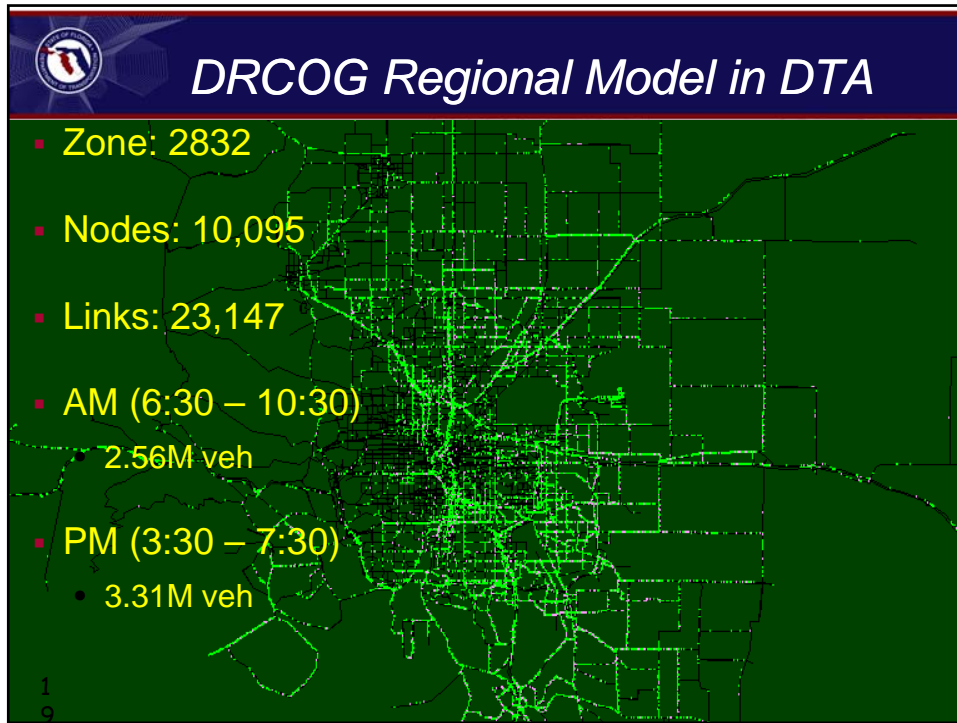
Credit: Jeff Shelton, TTI

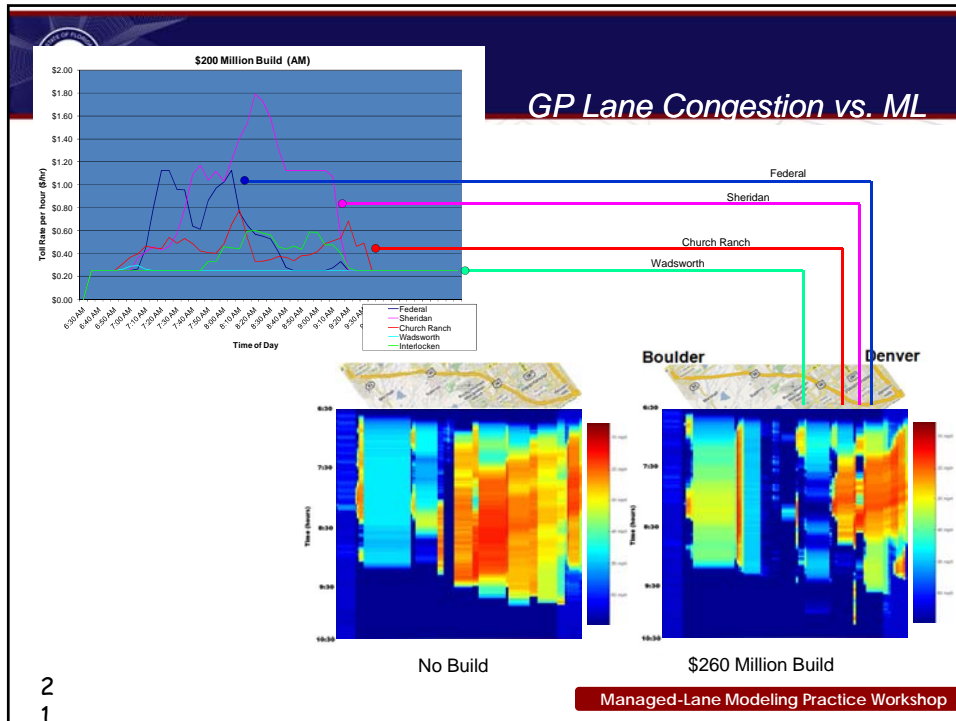
*Maximize throughput while maintaining target speed*

## Denver-Boulder US36 Congestion Pricing

- TIGER Applications
- Modeled 3 buildout strategies
- Estimated
  - Congestion
  - Revenue
  - Travel time
  - Fuel consumption
  - Emission

Managed-Lane






2  
1

## Addressing Heterogeneity

- Value-of-Time (VoT) plays a critical role in generalized cost type of DTA approach.
- VoT differs by trip purpose/socio-economic/location attributes.
- Increasing interesting in DTA and Activity-Based Model (ABM) integration
  - ABM produces trip/person specific VoT.

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2  
2




## Addressing Heterogeneity

- Existing approaches

<b>Discrete Choice Model</b> <ul style="list-style-type: none"> <li>- Individual route choice</li> <li>- Utility functions for toll and non-tolled routes</li> </ul>	<b>Multi-Class/Stratified Assignment</b> <ul style="list-style-type: none"> <li>- Stratify population by VoT distribution</li> <li>- Multi-class assignment for each VoT strata</li> </ul>
<b>Pros</b> <ul style="list-style-type: none"> <li>- Flexible, easy to implement</li> <li>- Computational efficient</li> </ul>	<b>Pros</b> <ul style="list-style-type: none"> <li>- Seek to converge</li> <li>- Stable results for scenario comparison</li> </ul>
<b>Cons</b> <ul style="list-style-type: none"> <li>- Hard to converge</li> <li>- Implication/interpretation</li> </ul>	<b>Cons</b> <ul style="list-style-type: none"> <li>- Computational demanding and becomes intractable with increasing problem size</li> </ul>

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## Summaries - Toll modeling with DTA

- Include alternate routes to model diversion
  - ✓ Static models do this well.
  - × Microsim not suitable for equilibrium DTA.
    - × Network too small.
    - × Not solving time-dependent shortest path.
  - ✓ DTA networks need to be large enough.
- Local congestion can affect tolls from far away
  - × Static models do not do queues and spillback.
  - ✓ Microsim has lots of detail.
  - ✓ DTA combines sufficient realism with larger-area networks.

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## Summary

- Advantage of applying DTA for pricing analysis appears to be obvious (hopefully).
- Various approaches are being offered for the following pricing schemes
  - Fixed toll
  - Time-of-day toll
  - Congestion responsive
- Addressing heterogeneity is desired
  - Ongoing research (SHRP2 L04, C10, etc.)
- Importance of feedback

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